

Vibronic Interaction and Vibrational Assignment for NO₃ in the Ground Electronic State

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VA-1. Stanton's ν_3 spurious ! (near 1000 cm^{-1} vs 1492 cm^{-1})

(1) IR absorption (Kawaguchi, Ishiwata, Hirota)

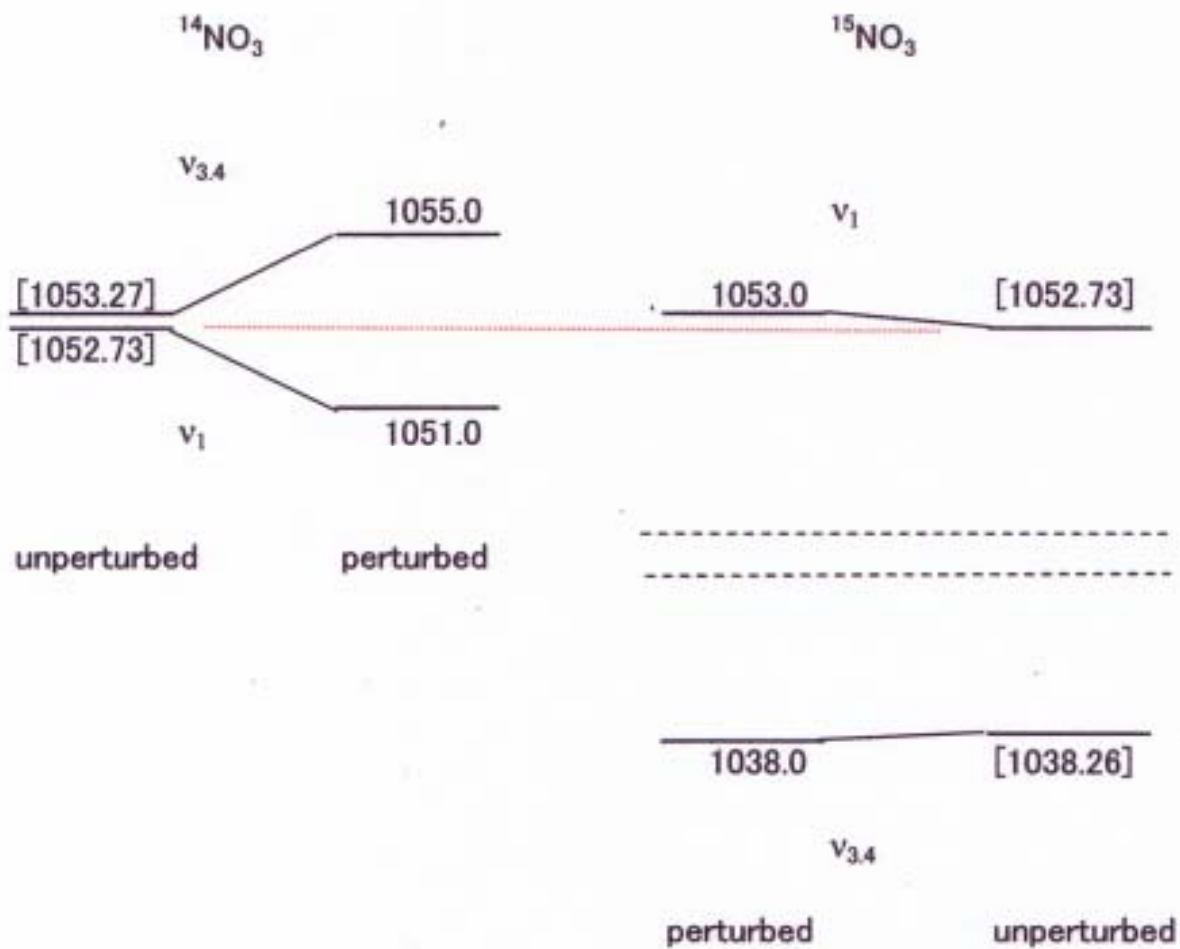
700~1500 cm^{-1} no ν_3 band

(2) LIF (Fukushima, Ishiwata)

	ν_1	“new”(cm^{-1})
$^{14}\text{NO}_3$	1051	1055
$^{15}\text{NO}_3$	1053	1038

“new” $\neq \nu_3$ no ν_3 band
 $= 3\nu_4(a')$

$$k_{1444} = 1.618, \nu_1^\circ = 1052.773$$



VA-2. only one $A-E$ type $Z-\nu_4$ hot band (Z: the upper state of the 1492 cm^{-1} band)

Assignment II Stanton-Jacox

$$Z = \nu_3 + \nu_4 \quad A_1, A_2, E$$

one $E-E$ and two $A-E$ are expected, but
no explanation has been given !

Assignment I traditional

$$Z = \nu_3, (2\nu_2)$$

one $E-E$: $\nu_3 - \nu_4$ and one $A-E$: $2\nu_2 - \nu_4$

$$\begin{aligned} \text{Cf. } \nu_2 &= 762.34045 \text{ (742.71195)} & (^{15}\text{NO}_3) \\ &\times 2 = 1524.6809 \text{ (1485.4239)} \end{aligned}$$

$$\text{Obs. } A-E \quad 1499.7493 \text{ (1475.1072)}$$

$$(4/3) \times [3\nu_4(a')]_{\text{av}} \quad 1512.(1488)$$

VA-3. Molecular parameters in Z, the upper state of the 1492 cm⁻¹ band

Assignment II ($\nu_3 + \nu_4$)

ν_4 l-type doubling const. q_4

obs. 0.001094 [cf. 0.0133024 in ν_4]

First-order Coriolis coupling constant ξ

obs. (*E* state) -0.19006 [$\xi_3 + \xi_4 = 0.0$]

No reasonable explanations have been provided,
indicating that

Assignment II is not acceptable !

VA-4. ν_4 progression in the photoelectron spectrum of NO_3^-

Neumark *et al.* (1991)

Herzberg-Teller effect via ν_4

Stanton (2007, 2009) ab initio

too large H-T parameters

distortion in PES of ν_4 in the GS

Stanton's anharmonicity constants excessive

No anomalies found in the ν_4 rot. structure

How can we explain the ν_4 progression by Assignment I ?

Our previous study on NO₃:

E. Hirota et al., *J. Chem. Phys.* **95**, 771 (1991)

Vibronic interaction between X^2A_2' and B^2E'

$$\mathbf{H}_{\text{ve}} = V_1 q \{ \exp[i(\theta - \alpha)] + \exp[-i(\theta - \alpha)] \} \\ + V_2 q^2 \{ \exp[i(\theta + 2\alpha)] + \exp[-i(\theta + 2\alpha)] \} + \dots$$

θ : unpaired electron, α : deg.normal mode(ν_3, ν_4)

2nd-order perturb. $h_1, h_2 \ll E(B - X) = 15000 \text{ cm}^{-1}$

$$h_1 = \langle B | V_1 | X \rangle, h_2 = \langle B | V_2 | X \rangle,$$

$$V_{\text{eff}} = (\omega/2)q^2 - (|h_1|^2/E)q^2 \\ - (|h_1 h_2|/E)(q_+^3 + q_-^3) + \dots$$

$$q_{\pm} = q \exp(\pm i \theta)$$

VR-1. Correlation between the first-order Coriolis coupling const. and the effective spin-orbit interaction constant

NOTE

These observations apply only to

Assignment I, but not to Assignment II !

Suggesting a new type of vibronic interaction

First-order Coriolis coupling constant and spin-orbit interaction constant $^{14}\text{NO}_3$

Band	$\nu_0^{\text{d)}$	ξ	$a_{\text{eff}}^{\text{e)}$
$\nu_4^{\text{a)}$	365.4840	−0.18743	−0.16888
$3\nu_4(E)^{\text{b)}$	1173.6141	−0.24887	−0.0991
$\nu_1 + \nu_4^{\text{b)}$	1413.5686	−0.11574	−0.13665
$\nu_3^{\text{a)}$	1492.39356	+0.19125	+0.17066
$\nu_1 + \nu_3^{\text{c)}$	2518.7130	+0.10190	+0.13290

^{a)}Present study.

^{b)}T. Ishiwata, unpublished.

^{c)}T. Ishiwata, I. Tanaka, K. Kawaguchi, and E. Hirota, *J. Mol. Spectrosc.* **153**, 167 (1992).

^{d)}Band origin, in cm^{-1} .

^{e)}Effective spin-orbit coupling constant $[a_{\text{eff}}L_cS_c]$, in cm^{-1} .

First-order Coriolis coupling constant and spin-orbit interaction constant $^{15}\text{NO}_3$

Band	$\nu_0^{\text{d)}$	ξ	$a_{\text{eff}}^{\text{e)}$
$\nu_4^{\text{a)}$	360.1996	−0.1557	−0.1657
$3\nu_4(E)^{\text{b)}$	1159.2456	−0.21122	−0.1065
$\nu_1 + \nu_4^{\text{b)}$	1407.0273	−0.06977	−0.12737
$\nu_3^{\text{a)}$	1472.8242	+0.1509	+0.1585
$\nu_1 + \nu_3^{\text{c)}$	2492.9587	+0.10306	+0.07876

^{a)}Present study.

^{b)}T. Ishiwata, unpublished.

^{c)}T. Ishiwata, Y. Nakano, K. Kawaguchi, E. Hirota, and I. Tanaka, *J. Phys. Chem. A***114**, 980 (2010).

^{d)}Band origin, in cm^{-1} .

^{e)}Effective spin-orbit coupling constant $[a_{\text{eff}}L_cS_c]$, in cm^{-1} .

VR-2. Harmonic force field
must include the contributions
of the unpaired electron

Care should be taken of this fact
in calculating isotopic shifts

Inertial defect and centrifugal distortion constant of NO₃ in the ground vibronic state

	Calc		obs
ξ_3	= 0.193	= 0.7	
Inertial defect(uÅ ²)	0.2221	0.2585	0.2193(64)
D_N (10 ⁻⁵ cm ⁻¹)	0.1069	0.1421	0.1058(49)
D_{NK} (10 ⁻⁵ cm ⁻¹)	-0.1965	-0.2667	-0.162(11)

VR-3. New-type of vibronic interaction

linear polyatomic free radical in $^2 \Sigma$

in excited state of bending $\rightarrow ^2 \Pi$

symmetric-top free radical in $^2 A$

in excited state of degenerate mode

$\rightarrow ^2 E$

bearing the character of a $^2 E$ excited
electronic state

So far almost no examples have been known !

VR.-4. A new vibronic interaction model (1)

Unpaired electron orbital in the ground electronic state

The a_2' orbital consists of

a radial part $R(r)$ and an azimuthal part $\Theta(\theta)$
in the A-type vibrational states

Θ has no θ dependence; cylindrical sym.

but, when a degenerate mode of E symmetry is
excited,

Θ includes a finite angular momentum
(electronic and vibrational), as defined by
$$\bar{\Lambda} = \Lambda + \ell = \pm 1$$

A new vibronic interaction model (2)

Total wavefunction: $|e\rangle|v\rangle|\bar{\Lambda}\rangle$,

rather than **conventional** $|e, \Lambda\rangle|v, \ell\rangle$

$|e\rangle|v\rangle$: only radial part

The effective spin-orbit term

mainly from the “diagonal” matrix elements

Degenerate vibrational states in the ground electronic state behave as degenerate electronic states, contribute to the photoelectron spectra of NO_3^- .

3 ν_4 states around 1050 cm⁻¹

isotopic species	¹⁴ NO ₃	¹⁵ NO ₃
3 $\nu_4(a')$ $ \ell_4 =3$	1055	1038
Diff.	122	122
3 $\nu_4(e')$ $ \ell_4 =1$	1177	1160
Diff.	37	34
3 $\nu_4(a')$ $ \ell_4 =3$	1214	1194
large splitting for $ \ell_4 =3$		
(2/3)[3 $\nu_4(a')$] _{av}	756	744
2 $\nu_4(a')$	754	744

Future

1. $\nu_2/2 \nu_4$ Coriolis interactions

No transitions have been assigned for $2 \nu_4$

2. Obs. and analysis of $3 \nu_4(a') - \nu_4$
and $\nu_1 - \nu_4$

3. New vibronic interaction

theoretical formulation required
on electron–nuclear interactions